# ANNEX J <br> Guidance for Determination of Necessary Bandwidth 

## J. 1 INTRODUCTION

This Annex contains guidance relating to the necessary bandwidth parameter. Necessary bandwidth forms part of the emission designator used for frequency management purposes and is used as a parameter in spectrum standards, frequency assignments, etc., throughout this Manual.

## J. 2 GENERAL

1. Except for radars, the necessary bandwidth may be determined by one of the following methods with the order of preference shown:
a. Use of the appropriate formula from Table A in this Annex. ${ }^{1}$
b. Computation in accordance with the Recommendations ITU-R SM.328-8 (1994) and SM. 853 (1994).
c. Measurements of specialized modulations not covered by 1 . or 2 . above.
d. Use of the best available technical information from other sources.
2. The value so determined shall be used when the full designation of an emission is required for example, as indicated in Chapter 9.
3. See Section 5.1.5 for the desired relationship of occupied bandwidth to necessary bandwidth.

## J. 3 RADAR SYSTEMS

For radars the necessary bandwidth shall be determined at a point that is 20 dB below the peak envelope value of the spectrum by one of the following with the order of preference shown:
a. Computation in accordance with the radar formulas from Table A in this Annex.
b. Results of actual measurement.
c. Use of the best available technical information from other sources.

## J. 4 ANALOG FM

1. The basis of the formulas in Table A for the necessary bandwidth of analog FM and FDM/FM systems is Carson's Rule. This bandwidth is given by $B_{1}=2(D+M)=2(a+1) M$, where D is the peak frequency deviation, " a " is the peak modulation index and M is the maximum modulating frequency. This rule represents an additive combination of the bandwidth expressions for extreme high ( $B_{1} \sim 2 D=2 a M$ ) and low ( $B_{1} \sim 2 M$ ) modulation index conditions. One of these two expressions prevails over the other for $\alpha \gg 1$ or $\alpha \ll 1$, so that their linear superposition always yields the bandwidth measure for extreme index conditions.
2. An accepted relationship between analog FM bandwidth and a measure of performance such as allowable distortion as a function of the modulation index is not available. There is no distortion measure or criterion that is generally accepted for evaluation purposes, because of difficulties arising from the variety of modulating signal characteristics and models that occur in practice.
3. The normalized FM bandwidth (B1/M) for single tone sinusoidal modulation is shown in Figure 1 for various power percentages included. Each stepped line corresponds to a fixed power percentage (p). The solid stepped line represents $\mathrm{p}=99 \%$ power included. The normalized bandwidth based on Carson's Rule is given by $(B 1 / M)=2(a+1)$, shown in Figure 1 by the solid straight line. Carson's Rule essentially follows the $p=99 \%$ line for indices in the $0.9<a<4.3$ range. It also includes more power at lower indices, but falls progressively below the $99 \%$ power curve at higher indices outside this range.
4. The case of a random modulating signal with a uniform baseband spectrum has also been analyzed using included power as the band-limiting distortion criterion. A peak to rms load ratio of 11 dB has been assumed to simulate representative conditions of FDM/FM telephony. The resultant normalized bandwidth can be estimated by $(\mathrm{B} 1 / \mathrm{M})=2 \mathrm{Z}(\mathrm{a}, \mathrm{q})$ where Z is a function of "a" and the fractional power rejected $\mathrm{q}=1-(\mathrm{p} / 100)$ as follows (Refs b

[^0]and c):
$$
Z(q, a)=a\left|\sqrt{1-\log _{\left(q^{5 / 7} 3^{3}\right)^{3}}-0.05}\right|+0.75
$$
5. This expression is an effective approximation to a complicated integral formulation for moderate index values $(1<a<5)$. The normalized bandwidth $(B 1 / M)$ is shown in Figure 2 for various (q) values, along with the bandwidth formula corresponding to Carson's Rule. The latter can be noted to represent a power rejection in the $10^{10}<q<10^{8}$ range, which is negligible.
6. The modulation cases shown in Figures 1 and 2 are extreme energy distribution conditions, in that one has all the baseband energy concentrated on a single frequency while the other has it spread uniformly over the baseband. The implication of Figures 1 and 2 is that Carson's Rule represents an effective bound to calculating analog FM bandwidth from a power included standpoint for modulation indices below five. The results also indicate that Carson's Rule includes considerably more power when the baseband modulation has a spread rather than concentrated spectral characteristic. Carson's Rule represents a $q=0.01$ power rejection for simple sinusoidal modulation, and $10{ }^{10}<q<10^{8}$ power rejection for a random modulation with a uniform baseband spectrum.
7. The necessary bandwidth of analog FM systems with modulation indices greater than 5.0 should be based on the methods of subparagraphs 2,3 and 4 of the above GENERAL section.

See References a, b, and c.

## J. 5 SYMBOLS

As appropriate, the following table shall be used for calculation of necessary bandwidth. The following symbols are used in this table:

| B | Digital symbol rate for telegraphy (i.e. baud) |
| :---: | :---: |
| $\mathrm{B}_{\mathrm{c}}=$ | Bandwidth of the frequency deviation (the total frequency shift during the pulse duration) in MHz. |
| $\mathrm{B}_{\mathrm{d}}=$ | Bandwidth of the frequency deviation (peak difference between instantaneous frequency of the modulated wave and the carrier frequency for FM/CW radar systems) |
| $\mathrm{B}_{\mathrm{n}}=$ | Necessary bandwidth |
| $\mathrm{C}=$ | Sub-carrier frequency |
| $\mathrm{C}_{\text {max }}=$ | Highest sub-carrier frequency used. |
| $\mathrm{C}_{\text {S }}=$ | Separation in frequency between adjacent sub-carriers or carriers of a multi-carrier modulation. |
| $\mathrm{D}=$ | Peak deviation, i.e., half the difference between the maximum and minimum values of the instantaneous frequency. |
| $\mathrm{f}_{\mathrm{p}}=$ | Continuity pilot sub-carrier frequency (continuous signal utilized to verify performance of frequency-division multiplex systems). |
| $\mathrm{K}=$ | An overall numerical factor which varies according to the emission and which depends upon the allowable signal distortion. |
| $\mathrm{M}=$ | Maximum modulation frequency |
| $\mathrm{N}_{\mathrm{c}}=$ | Number of baseband channels in radio systems employing multichannel multiplexing. |
| $\mathrm{N}_{\mathrm{s}}=$ | Number of Sub-carriers. |
| $\mathrm{R}=$ | Total bit rate, which includes data, encoding, and any other overhead bits. |
| S $=$ | Number of equivalent non-redundant signaling states. |
| t $=$ | Emitted pulse duration in $\mu \mathrm{sec}$ at $50 \%$ amplitude (voltage) points. The $100 \%$ amplitude is the nominal peak level of the pulse. |
| $\mathrm{t}_{\mathrm{f}}=$ | Emitted pulse fall time in $\mu$ sec from the $90 \%$ to the $10 \%$ amplitude points on the trailing edge. |
| $\mathrm{t}_{\mathrm{r}}=$ | Emitted pulse rise time in $\mu \mathrm{sec}$ from the $10 \%$ to the $90 \%$ amplitude points on the leading edge. |
| $\mathrm{X}=$ | Average "talker power level" (in dBm0) used to determine the peak frequency deviation in FM/FDM systems. These values are normally specified by the equipment manufacturer (see Table B later in this annex for more information). |



Figure 1: FM Bandwidth Occupancy and Power Preservation with Sinusoidal Modulation (Note: Carson's Rule is the Straight Line)
(Legend: p is the Power Percentage Preserved)


Figure 2: FM Bandwidth Occupancy and Power Preservation with Band-Limited White Modulation
(Note: Carson's Rule is the Dotted Line)
(Legend: $\mathbf{q}$ is the Power Fraction Rejected)

## Table A: Necessary Bandwidth Calculations

| Description of Emission | Formula | Sample Calculation | Sample Emission Designator |
| :---: | :---: | :---: | :---: |
| NO MODULATION |  |  |  |
| Continuous wave emission | $\mathrm{B}_{n}=0$ | Satellite downlink beacon | N0N |
| CW radars ${ }^{2}$ | $\mathrm{B}_{n}=0$ | Speed measuring CW radar $\mathrm{B}_{n}=0 \mathrm{~Hz}$ | 0H00N0N |
| ANALOG |  |  |  |
| Amplitude Modulation |  |  |  |
| Broadcasting |  |  |  |
| Sound broadcasting, double-sideband | $B_{n}=2 M$ <br> $M$ may vary between 4000 and 10000 depending on the quality desired. | $\begin{gathered} \text { Speech and music } \\ M=4000 \\ B_{n}=8000 \mathrm{~Hz}=8 \mathrm{kHz} \\ \hline \end{gathered}$ | 8K00A3EGN |
| Sound broadcasting, single-sideband, suppressed carrier | $B_{n}=M$ (lowest modulation frequency) | $\begin{gathered} \text { Speech and music } \\ M=4500 \\ \text { lowest modulation frequency }=50 \mathrm{~Hz} \\ B_{n}=4450 \mathrm{~Hz}=4.45 \mathrm{kHz} \\ \hline \end{gathered}$ | 4K45J3EGN |
| Sound broadcasting, singlesideband, reduced carrier | $B_{n}=M$ $M$ may vary between 4000 and 10000 depending on the quality desired | $\begin{gathered} \text { Speech and music } \\ M=4000 \\ B_{n}=4000 \mathrm{~Hz}=4 \mathrm{kHz} \\ \hline \end{gathered}$ | 4K00R3EGN |

[^1]| Description of Emission | Formula | Sample Calculation | Sample Emission Designator |
| :---: | :---: | :---: | :---: |
| (single channel) |  |  |  |
| Radio Relay |  |  |  |
| Double-sideband radiorelay system, frequency division multiplex | $B_{n}=2 M$ | 10 voice channels occupying base band between 1 kHz and 164 kHz $\begin{gathered} M=164000 \\ B_{n}=328000 \mathrm{~Hz}=328 \mathrm{kHz} \\ \hline \end{gathered}$ | 328K00A8E |
| Double-sideband, television relay | $B_{n}=2 C+2 M+2 D$ | Video limited to 5 MHz , audio on 6.5 MHz frequency modulated subcarrier, sub-carrier deviation $=50 \mathrm{kHz}$ : $\begin{gathered} C=6.5 \times 10^{6} \quad D=50 \times 10^{3} \mathrm{~Hz} \\ M=15000 \\ B_{n}=13.13 \times 10^{6} \mathrm{~Hz}=13.13 \mathrm{MHz} \end{gathered}$ | 13M13A8W |
| Telephony |  |  |  |
| Telephony, double sideband (single channel) | $B_{n}=2 M$ | $\begin{gathered} M=3000 \\ B_{n}=6000 \mathrm{~Hz}=6 \mathrm{kHz} \end{gathered}$ | 6K00A3EJN |
| Telephony, independent sideband (two or more channels) | $B_{n}=$ sum of $M$ for each side band | $\begin{gathered} 2 \text { channels } \\ M=3000 \\ B_{n}=6000 \mathrm{~Hz}=6 \mathrm{kHz} \\ \hline \end{gathered}$ | 6K00B8EJN |
| Telephony, single-sideband, full carrier (single channel) | $B_{n}=M$ | $\begin{gathered} M=3000 \\ B_{n}=3000 \mathrm{~Hz}=3 \mathrm{kHz} \end{gathered}$ | 3K00H3EJN |
| Telephony, single-sideband, suppressed carrier (single channel) | $B_{n}=M$ (lowest modulation frequency) | $M=3000$ <br> lowest modulation frequency $=300 \mathrm{~Hz}$ $B_{n}=2700 \mathrm{~Hz}=2.7 \mathrm{kHz}$ | 2K70J3EJN |
| Telephony with privacy, singlesideband, suppressed carrier (two or more channels) | $\mathrm{B}_{\mathrm{n}}=\mathrm{N}_{\mathrm{c}} \mathrm{M}$ <br> (lowest modulation frequency in the lowest channel) | $\begin{gathered} \hline N c=2 \\ M=3000 \\ \text { lowest modulation frequency }=250 \mathrm{~Hz} \\ B_{n}=5750 \mathrm{~Hz}=5.75 \mathrm{kHz} \\ \hline \end{gathered}$ | 5K75J8EKF |
| Telephony with separate frequency modulated signal to control the level of demodulated speech signal, single- sideband, reduced carrier (Lincompex) (single channel) | $B_{n}=M$ | Maximum control frequency $=2990 \mathrm{~Hz}$ $\begin{gathered} M=2990 \\ B_{n}=2990 \\ \mathrm{~Hz}=2.99 \mathrm{kHz} \end{gathered}$ | 2K99R3ELN |
| Television |  |  |  |
| Television, vision and sound | Refer to Recommendations ITU-R <br> BT. 470 and BO. 650 for the bandwidths of the commonly used television systems. ${ }^{3}$ | Number of lines = 525 <br> Number of lines per second $=15,750$ <br> Video bandwidth: 4.2 MHz <br> Total visual bandwidth: 5.75 MHz <br> FM aural bandwidth including guard bands: 250 kHz <br> Total bandwidth: 6 MHz | $\begin{gathered} \text { 5M75C3F } \\ \text { 250K0F3EGN } \end{gathered}$ |
| Miscellaneous |  |  |  |
| Double-sideband emission of VOR with voice <br> (VOR: VHF omnidirectional radio range) | $\begin{gathered} B_{n}=2 C_{\max }+2 M+2 D K \\ K=1 \text { (typically) } \end{gathered}$ | The main carrier is modulated by: a 30 Hz sub-carrier <br> a carrier resulting from a 9960 Hz tone frequency modulated by a 30 Hz tone a telephone channel a 1020 Hz keyed tone for con tinual Morse identification $C_{\max }=9960$ $M=30 \quad D=480 \mathrm{~Hz}$ $B_{n}=20940 \mathrm{~Hz}=20.94 \mathrm{kHz}$ | 20K9A9WWF |
| Angle Modulation |  |  |  |
| Broadcasting |  |  |  |
| Sound broadcasting | $\begin{aligned} & B_{n}=2 M+2 D K \\ & K=1 \text { (typically) } \end{aligned}$ | $\begin{gathered} \text { Monaural } \\ D=75000 \mathrm{~Hz} \\ M=15000 \end{gathered}$ | 180KF3EGN |

3 ITU-R Recommendations and other publications are available on the internet at http://www.itu.int/ITU-R/pub lications/index.html.

| Description of Emission | Formula | Sample Calculation | Sample Emission Designator |
| :---: | :---: | :---: | :---: |
|  |  | $B_{n}=180000 \mathrm{~Hz}=180 \mathrm{kHz}$ |  |
| Stereophonic sound broad casting with multiplexed subsidiary telephony subcarrier | $\begin{gathered} B_{n}=2 M+2 D K \\ K=1 \text { (typically) } \end{gathered}$ | $\begin{gathered} \hline \text { Pilot tone system; } \\ M=75000 \\ D=75000 \mathrm{~Hz} \\ B_{n}=300000 \mathrm{~Hz}=300 \mathrm{kHz} \\ \hline \end{gathered}$ | 300K0F8EHF |
| Radar |  |  |  |
| FM/CW radars | $\mathrm{B}_{n}=2 \mathrm{~B}_{\mathrm{d}}$ | FM-CW Doppler radar sweeps $\pm 100 \mathrm{MHz}$ from center frequency over a sweep duration of 50 msec . $\mathrm{B}_{n}=200 \mathrm{MHz}$ | 200MF3N |
| Radio Relay |  |  |  |
| Radio-relay system; frequency division multiplex | $\begin{gathered} B_{n}=2 \mathrm{M}+2 \mathrm{DK} \\ \mathrm{~K}=1 \text { (typically) } \end{gathered}$ | 960 data channels that operate at a uniform power level of - 15 dBm occupying baseband between 60 kHz and 4028 kHz ; rms per channel deviation: 200 kHz ; continuity pilot at 4715 kHz produces 140 kHz rms deviation of main carrier. ${ }^{4}$ $\begin{gathered} \mathrm{X}=-15 \\ \mathrm{D}=\left(200 \times 10^{3}\right)(3.76)(5.5)=4.14 \times 10^{6} \mathrm{~Hz} ; \\ \mathrm{M}=4.028 \times 10^{6} ; \\ \mathrm{f}_{\mathrm{p}}=4.715 \times 10^{6},(2 \mathrm{M}+2 \mathrm{DK})>2 \mathrm{f}_{\mathrm{p}} \\ \mathrm{~B}_{n}=16.34 \times 10^{6} \mathrm{~Hz}=16.34 \mathrm{MHz} \\ \hline \end{gathered}$ | 16M4F8DJF |
| Radio-relay system, frequency division multiplex | $B_{n}=2 f_{p}$ | 600 telephone channels occupying baseband between 60 kHz and 2540 kHz; <br> rms per-channel deviation: 200 kHz continuity pilot at 8500 kHz produces 1440 kHz rms deviation of main carrier. $\text { For } \mathrm{X}=-19.6 \text { : }$ $\begin{gathered} D=\left(200 \times 10^{3}\right)(3.76)(2.56)=1.93 \times 10^{6} \mathrm{~Hz} \\ M=2.54 \times 10^{6} \\ K=1 \\ f_{p}=8.5 \times 10^{6} \end{gathered}$ <br> Use $2 f_{p}$ since it is $>(2 \mathrm{M}+2 \mathrm{DK}) 4$ $\mathrm{Bn}=17 \times 10^{6} \mathrm{~Hz}=17 \mathrm{MHz}$ | 17M0F8EJF |
| Radio-relay systems, frequency division multiplex | $\begin{gathered} B_{n}=2 f_{p}+2 \mathrm{DK} \\ \mathrm{~K}=1 \text { (typically) } \end{gathered}$ | 60 all voice telephone channels occupying baseband between 60 kHz and 300 kHz ; rms per-channel deviation: 200 kHz ; continuity pilot at 331 kHz produces 100 kHz rms deviation of main carrier For $\mathrm{X}=-5.6$ : $\begin{gathered} \mathrm{D}=\left(200 \times 10^{3}\right)(3.76)(1.19)=8.95 \times 10^{5} \mathrm{~Hz} ; \\ \mathrm{M}=0.3 \times 10^{6} \\ f_{p}=0.331 \times 10^{6} \mathrm{~Hz} \end{gathered}$ <br> Use $2 f_{p}+2$ DK since $f_{p}>$ M. 4 $\mathrm{B}_{n}=2.45 \times 10^{6} \mathrm{~Hz}=2.45 \mathrm{MHz}$ | 2M45F8EJF |
| Telephony |  |  |  |
| Commercial telephony | $B_{n}=2 M+2 D K$ <br> $K=1$ (typically, but under certain conditions a higher value of $K$ may be necessary) | For an average case of commercial telephony, $\begin{gathered} D=5000 \mathrm{~Hz} \\ M=3000 \\ B_{n}=16000 \quad \mathrm{~Hz}=16 \mathrm{kHz} \end{gathered}$ | 16K0F3EJN |
| Aeronautical Mobile Telemetry |  |  |  |
| Filtered non-return-to-zero <br> (NRZ) pulse code modulation/frequency modulation (PCM/FM) | $B_{n}=1.16 \mathrm{R}$ <br> with $2 \mathrm{D} / \mathrm{R}=0.7$ <br> And premodulation filter bandwidth $=0.7 \mathrm{R}$ | Digital modulation used to send 5 megabits per second using frequency modulation with 2 signaling states and 1.75 MHz peak deviation $\mathrm{R}=5 \times 10^{6} ; \mathrm{B}_{\mathrm{n}}=5.8 \mathrm{MHz}$ | 5M80F1D |
| Constant envelope offset | $B_{n}=0.78 \mathrm{R}$ | Digital modulation used to send 5 | 3M90G1D |

See the Table B instructions.

| Description of Emission | Formula | Sample Calculation | Sample Emission Designator |
| :---: | :---: | :---: | :---: |
| quadrature phase shift keying; Feher’s patented quadrature phase shift keying (FQPSK-B, FQPSKJR) or shaped offset quadrature phase shift keying (SOQPSK-TG) |  | megabits per second using offset quadrature phase shift keying with 4 signaling states $\mathrm{R}=5 \times 10^{6} ; \mathrm{B}_{\mathrm{n}}=3.9 \mathrm{MHz}$ |  |
| Advanced Range Telemetry (ARTM) continuous phase modulation (ARTM CPM) | $B_{n}=0.56 \mathrm{R}$ <br> With modulation index $=4 / 16$ and $5 / 16$ on alternating symbols | Digital modulation used to send 5 megabits per second using frequency modulation with 4 signaling states and with alternating modulation index each symbol $\mathrm{R}=5 \times 10^{6} ; \mathrm{B}_{\mathrm{n}}=2.8 \mathrm{MHz}$ | 2M80F1D |
| Digital |  |  |  |
| Amplitude Modulation |  |  |  |
| Telegraphy |  |  |  |
| Continuous wave telegraphy, Morse code | $\begin{gathered} \mathrm{B}_{n}=\mathrm{BK} \\ K=5 \text { for fading circuits } \\ K=3 \text { for non-fading circuits } \end{gathered}$ | 25 words per minute $\begin{aligned} & B=20, K=5 \\ & B_{n}=100 \mathrm{~Hz} \\ & \hline \end{aligned}$ | 100H0A1AAN |
| Telegraphy by on-off key ing of a tone modulated car rier, Morse code | $\begin{gathered} B_{n}=B K+2 M \\ K=5 \text { for fading circuits } \\ K=3 \text { for non-fading circuits } \end{gathered}$ | $\begin{gathered} 25 \text { words per minute } \\ B=20, M=1000, K=5 \\ B_{n}=2100 \quad \mathrm{~Hz}=2.1 \mathrm{kHz} \end{gathered}$ | 2K10A2AAN |
| Independent sidebands; sev eral telegraph channels with error-correction together with several telephone channels with privacy; frequency division multiplex | $B_{n}=$ sum of $M$ for each sideband | Normally composite systems are operated in accordance with standardized channel arrangements (e.g. Rec. ITU-R F.348). <br> 3 telephone channels and 15 telegraphy channels require the bandwidth: $12000 \mathrm{~Hz}=12 \mathrm{kHz}$ | 12K0B9WWF |
| Selective calling signal using sequential single frequency code, single-sideband full carrier | $B_{n}=M$ | Maximum code frequency is: 2110 Hz $\begin{gathered} M=2110 \\ B_{n}=2110 \mathrm{~Hz}=2.11 \mathrm{kHz} \end{gathered}$ | 2K11H2BFN |
| Direct-printing telegraphy using a frequency shifted modulating sub-carrier, with error-correction, single-side band, suppressed carrier (single channel) | $\begin{gathered} B_{n}=2 M+2 D K \\ M=\frac{B}{2} \end{gathered}$ | $\begin{gathered} B=50 \\ D=35 \mathrm{~Hz}(70 \mathrm{~Hz} \text { shift }) \\ K=1.2 \\ B_{n}=134 \mathrm{~Hz} \end{gathered}$ | 134H0J2BCN |
| Telegraphy, multichannel with voice frequency, error correction, some channels are time-division multi plexed, single-sideband, reduced carrier | $\begin{gathered} B_{n}=(\text { highest central frequency })+M \\ +D K \\ M=\frac{B}{2} \end{gathered}$ | 15 channels; highest central frequency is: 2805 Hz $\begin{gathered} B=100 \\ D=42.5 \mathrm{~Hz}(85 \mathrm{~Hz} \text { shift }) \\ K=0.7 \\ B_{n}=2885 \mathrm{~Hz}=2.885 \mathrm{kHz} \\ \hline \end{gathered}$ | 2K89R7BCW |
| Angle Modulation |  |  |  |
| Telegraphy |  |  |  |
| Telegraphy, narrow-band direct-printing with error correction (single channel) or Selective calling signal | $\begin{gathered} B_{n}=2 M+2 D K \\ M=\frac{B}{2} \\ K=1.2 \text { (typically) } \end{gathered}$ | $\begin{gathered} B=100 \\ D=85 \mathrm{~Hz}(170 \mathrm{~Hz} \text { shift }) \\ B_{n}=304 \mathrm{~Hz} \end{gathered}$ | 304H0F1BCN |
| Telegraphy without errorcorrection (single channel) | $\begin{gathered} B_{n}=2 M+2 D K \\ M=\frac{B}{2} \\ K=1.2 \text { (typically) } \\ \hline \end{gathered}$ | $\begin{gathered} B=100 \\ D=85 \mathrm{~Hz}(170 \mathrm{~Hz} \text { shift }) \\ B_{n}=304 \mathrm{~Hz} \end{gathered}$ | 304H0F1BBN |
| Four-frequency duplex telegraphy | $\begin{aligned} & B_{n}=2 M+2 D K \\ & B=\text { modulation rate in bauds of the } \\ & \text { faster channel. } \\ & \text { If the channels are synchronized: } \end{aligned}$ | Spacing between adjacent frequencies $=400 \mathrm{~Hz}$ Synchronized channels $\begin{aligned} & B=100 \\ & M=50 \end{aligned}$ | 1K42F7BDX |


| Description of Emission | Formula | Sample Calculation | Sample Emission Designator |
| :---: | :---: | :---: | :---: |
|  | $\begin{gathered} M=\frac{B}{2} \\ \text { (otherwise, } M=2 B \text { ) } \\ K=1.1 \text { (typically) } \end{gathered}$ | $\begin{gathered} D=600 \mathrm{~Hz} \\ B_{n}=1420 \mathrm{~Hz}=1.42 \mathrm{kHz} \end{gathered}$ |  |
| Miscellaneous |  |  |  |
| Binary Frequency Shift Keying ${ }^{5}$ | If $\quad 0.03<\frac{2 D}{R}<1.0 \quad$ Then $B_{n}=3.86 D+0.27 R$ <br> If $\quad 1.0<\frac{2 D}{R}<20$ <br> Then $B_{n}=2.4 D+1.0 R$ | Digital modulation used to send 1 megabit per second by frequency shift keying with 2 signaling states and 0.75 MHz peak deviation of the carrier. $\begin{gathered} \mathrm{R}=1 \times 10^{6} \text { bits per second; } \\ \mathrm{D}=0.75 \times 10^{6} \mathrm{~Hz} ; \\ \mathrm{B}_{n}=2.8 \mathrm{MHz} \end{gathered}$ | 2M80F1DBC |
| Multilevel Frequency Shift Keying | $\begin{gathered} B_{n}=\frac{R}{\log _{2} S}+2 D K \\ K \leq 0.89 \\ \left(99 \% \text { bandwidth, Bn=R/ } \log _{2} \mathrm{~S}+\right. \\ 1.78 \mathrm{D}) \end{gathered}$ | Digital modulation to send 10 Mbps by use of frequency shift keying with 4 signaling states and 2 MHz peak deviation of the main carrier. $\begin{gathered} \mathrm{R}=10^{7} \mathrm{bps} ; \\ \mathrm{D}=2 \mathrm{MHz} ; \\ \mathrm{K}=0.89 ; \\ \mathrm{S}=4 ; \quad \mathrm{B}_{n}=8.56 \mathrm{MHz} \\ \hline \end{gathered}$ | 8M56F1DDT |
| Gaussian Minimum Shift Keying (GMSK) | $\begin{gathered} B_{n}=\frac{R}{\log _{2} S}+0.5 R K \\ K \leq-0.28 \\ \left(99 \% \text { bandwidth, } \mathrm{B}_{n}=\left(1 / \log _{2} \mathrm{~S}-\right.\right. \\ 0.14) \mathrm{R}) \end{gathered}$ | Digital modulation used to send 10 megabits per second by use of GMSK ( $\mathrm{S}=2$ ) $\mathrm{R}=10 \times 10^{6} \text { bits per second; }$ $\mathrm{B}_{n}=8.6 \mathrm{MHz}$ | 8M60G1DDN |
| Minimum Shift Keying | $\begin{gathered} B_{n}=\frac{R}{\log _{2} S}+0.5 R K \\ K \leq 0.36 \\ (99 \% \text { bandwidth, } \\ \left.B_{n}=\left(1 / \log _{2} S+0.18\right) R\right) \end{gathered}$ | Digital modulation used to send 2 megabits per second using 2-ary minimum shift keying: $\begin{gathered} \mathrm{R}=2 \mathrm{Mbps} \\ \mathrm{~S}=2 \\ \mathrm{~B}_{n}=2.36 \times 10^{6} \mathrm{~Hz}=2.36 \mathrm{MHz} \end{gathered}$ | 2M36G1DBN |
| Feher-patented <br> Quadrature Phase Shift <br> Keying (FQPSK-B) | $B_{n}=0.78 R$ | Digital modulation to send 10 megabits per second by use of FQPSK-B $R=10 \times 10^{6}$ bits per second; $\mathrm{B}_{n}=7.8 \mathrm{MHz}$ | 7M80G1DDN |
| Phase Shift Keying | $\begin{gathered} B_{n}=2 R K / \log _{2} S \\ 0.5 \leq \mathrm{K} \leq 1 \\ \mathrm{~K}=0.7 \text { to } 0.8 \text { (typically) }^{6} \end{gathered}$ | Digital modulation used to send 10 megabits per second by use of phase shift keying with <br> 4 signaling states $\begin{gathered} \mathrm{R}=10 \times 10^{6} \text { bits per second; } \\ \mathrm{K}=1 ; \mathrm{S}=4 ; \\ \mathrm{B}_{n}=10 \mathrm{MHz} \end{gathered}$ | 10M00G1DDT |
| Combination Modulation |  |  |  |
| Quadrature Amplitude <br> Modulation (QAM) | $B_{n}=\frac{2 R K}{\log _{2} S}$ $K \leq 0.81$ <br> (99\% bandwidth, $\left.B_{n}=1.62 R / \log _{2} S\right)$ | 64 QAM is used to send 135 Mbps ; $\begin{gathered} \mathrm{R}=135 \times 10^{6} \mathrm{bps} ; \\ \mathrm{S}=64 ; \\ \text { Roll-off = } 1 ; \\ \mathrm{K}=0.81 \\ \mathrm{~B}_{n}=36.45 \mathrm{MHz} \end{gathered}$ | 36M45D1D |
| Orthogonal Frequency | $B_{n}=\left(N_{S}+16.25\right) C_{S}$ | OFDM is used to send 20 Mbps . Guard time | 16M1D1DEF |

5 See References g, h, and i for further details.
${ }^{6} \quad$ The value for K here can theoretically vary from 0.5 to 1 . For fixed microwave systems use of a value of K larger than 0.7 should be further justified.

| Description of Emission | Formula | Sample Calculation | Sample Emission Designator |
| :---: | :---: | :---: | :---: |
| Division Multiplexing (OFDM) | $N_{S}>16$ | is $0.8 \mu \mathrm{~s} .48$ sub-carriers are used, each spaced 250 kHz apart. 16-QAM is used with rate $1 / 2$ coding. $\mathrm{B}_{n}=(48+16.25) 0.25=16.1 \mathrm{MHz}$ |  |
| PULSED |  |  |  |
| Radar |  |  |  |
| Non-FM pulsed radars (including spread spectrum or coded pulse radars): ${ }^{7}$ | $\begin{gathered} \text { If } \frac{t}{t_{r}} 12.6 \text {, then: } \\ B_{n}=B(-20 d B)={\frac{1.79}{\sqrt{t_{r} t}}}^{8} \end{gathered}$ <br> Otherwise: $B_{n}=B(-20 d B)=\frac{6.36}{t}$ | A radar transmits unmodulated pulses at 1172 pulses per sec. The pulse width is 1.03 usec. Rise and fall times are $0.2 \mu \mathrm{sec}$ and $0.15 \mu \mathrm{sec}$, respectively. <br> Use $t_{f}$ since it is smaller than $t_{r}$ Since $t$ is obviously less than $12.6 \mathrm{t}_{\mathrm{f}}$, use the first equation $\mathrm{B}_{n}=4.55 \mathrm{MHz}$ | 4M55P0N |
| Phase coded pulse radars (including spread spectrum): ${ }^{7}$ | If $\frac{t}{t_{r}} 12.6$ then: $B_{n}=B(-20 d B)=\frac{1.79}{\sqrt{t_{r} t}}, 8^{, 9}$ <br> Otherwise: $B_{n}=B(-20 d B)=\frac{6.36}{\sqrt{t}}$ | A Doppler pulse radar transmits 3000 pulses per second. The pulse width including a 13 bit Barker code is $6.6 \mu \mathrm{sec}$. Each chip has a $50 \%$ amplitude width of $0.5 \mu \mathrm{sec}$. Chip rise time is $0.02 \mu \mathrm{sec}$. <br> Since $\mathrm{t} / \mathrm{t}_{\mathrm{r}}=0.5 / 0.02$ is obviously larger than 12.6, use the second equation: $B_{n}=6.36 / 0.5=12.7 \mathrm{MHz}$ | 12M7Q1N |
| FM-pulse radars (intentional FM) ${ }^{7}$ | $B_{n}=B(-20 d B)=\frac{1.79}{\sqrt{t_{r} t}}+2 B_{c}{ }^{8}$ | FM pulsed radar chirping over 2.89 MHz with a $25.6 \mu \mathrm{sec}$ pulse width and 150 nsec rise time $\mathrm{B}_{n}=6.69 \mathrm{MHz}$ | 6M69Q3N |
| Composite Emissions |  |  |  |
| Radio-relay system | $\begin{aligned} & B_{n}=\frac{2 K}{t} \\ & \mathrm{~K} \leq 1.6^{10} \end{aligned}$ | Pulse position modulated by 36 voice channel baseband; pulse width at half $\begin{gathered} \text { amplitude }=0.4 \mu \mathrm{sec} \\ B_{n}=8 \quad 10^{6} \mathrm{~Hz}=8 \mathrm{MHz} \end{gathered}$ <br> (Bandwidth independent of the number of voice channels) | 8M00M7EJT |
| Composite transmission digital modulation using DSB- AM <br> (Microwave radio relay system) | $\mathrm{B}_{\mathrm{n}}=2 \mathrm{RK} / \log _{2} S$ | Digital modulation used to send 5 megabits per second by use of amplitude modulation of the main carrier with 4 signaling states $\begin{gathered} \mathrm{R}=5 \times 10^{6} \text { bits per second; } \\ \mathrm{K}=1 ; \mathrm{S}=4 \\ \mathrm{~B}_{n}=5 \mathrm{MHz} \\ \hline \end{gathered}$ | 5M00K7DD |

7 For frequency hopping systems the necessary bandwidth is the instantaneous one of an individual channel.
8 If $t_{f}$ is less than $t_{r}$, then $t_{f}$ is to be used in place of $t r$ when performing the necessary bandwidth calculations.
$9 \quad$ For phase coded pulse signals the pulse width and rise times are those associated with a single sub-pulse. If the rise time of a single sub-pulse is not available, assume it is $40 \%$ of the time to switch from one phase or sub-pulse to the next (see Figure 1)
${ }^{10}$ In this case $K$ depends upon the ratio of pulse width to pulse rise time. Its value usually falls between 1 and 10 and in many cases does not need to exceed $6 . \mathrm{K}=1.6$ roughly corresponds to rise time equal to pulse width, which is typical for these systems.


Figure 3: Estimation of chip rise time for phase coded pulse signals
Table B: Multiplying Factors for Use in Computing D, Peak Frequency Deviation, in Fm
Frequency Division Multiplex (Fm/Fdm) Multi-Channel Emissions

1. For FM/FDM systems the necessary bandwidth is (for systems having no continuity pilot sub-carrier or having a continuity pilot sub-carrier whose frequency is not the highest modulating the main carrier):

$$
\mathrm{Bn}=2 \mathrm{M}+2 \mathrm{DK}
$$

2. The value of D , or peak frequency deviation, in these formulas for Bn is calculated by multiplying the rms value of per-channel deviation by the appropriate "multiplying factor" shown below.
3. In the case where a continuity pilot of frequency fp exists above the maximum modulation frequency, M , the general formula becomes:
Bn = 2fp + 2DK
4. In the case where the modulation index of the main carrier produced by the pilot is less than 0.25 , and the rms frequency deviation of the main carrier produced by the pilot is less than or equal to 70 percent of the rms value of per-channel deviation, or in a radio system for television, the rms deviation of the main carrier due to the pilot does not exceed 3.55 percent of the peak deviation of the main carrier, the general formula becomes either: $\mathrm{Bn}=2 \mathrm{fp}$ or $\mathrm{Bn}=2 \mathrm{M}+2 \mathrm{DK}$ whichever is greater.
5. The selection of the values used to determine the multiplying factor are highly dependent upon the information transfer requirements placed upon the FM/FDM systems. Available technical information indicates that (depending on the number of channels) a value of "X" of -2 , -5.6 or -19.6 should be appropriate for modern commercial telephone circuits where most of the channels are actual speech. In smaller or older FM/FDM systems and those where most of the circuits are used for data transmission, " X " values of $+2.6,-1.0$ or -15 should be appropriate since typical commercial multichannel data circuits operate at power levels from -13 to -15 dBm0.

| Number telephone channels $\mathbf{N}_{\mathbf{c}}$ | Multiplying factors | Limits of $\mathrm{X}\left(\mathrm{P}_{\mathrm{avg}}(\mathrm{dBm} 0)\right.$ |
| :---: | :---: | :---: |
| $3<\mathrm{N}_{\mathrm{c}}<12$ | $4.47 \mathrm{x} \text { antilog } \mathrm{x} \frac{x}{20}$ <br> $\mathrm{X}=\mathrm{a}$ value in dB specified by the equipment manufacturer or station licensee, subject to NTIA approval | Not applicable |
| $12<\mathrm{N}_{\mathrm{c}}<60$ | $3.76 \text { antilog } \frac{\left(\mathrm{X}+2 \log _{10} \underline{\mathrm{~N}}_{\mathrm{c}}\right)}{20}$ | X: -2 to +2.6 |
| $60<\mathrm{N}_{\mathrm{c}}<240$ | $3.76 \text { antilog } \frac{\left(\mathrm{X}+4 \log _{10} \mathrm{~N}_{\mathrm{c}}\right)}{20}$ | X: -5.6 to -1.0 |
| $\mathrm{N}_{\mathrm{c}}>240$ | $\left.3.76 \text { antilog } \frac{(\mathrm{X}+10}{20} \log _{10} \mathbf{N}_{\mathrm{G}}\right)$ | X: -19.6 to -15.0 |

Where Nc is the number of circuits in the multiplexed message load; 4.47 corresponds to a peak load factor of 13.0 dB , and 3.76 corresponds to a peak load factor of 11.5 dB .

## J. 6 References

The following is a list of reference documents:
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[^0]:    ${ }^{1}$ Individual formulas may be based on theoretical models for the modulation technique.

[^1]:    ${ }^{2}$ The emission bandwidth of a CW transmitter typically will not be zero due to noise and other considerations. However, designating zero as the necessary bandwidth is a valid method for identifying such equipment.

